Hash Tables and Hashing

EECS 214, Fall 2017

Dictionary data structures we have seen, with lookup times and a special case

- Binary search tree $\mathcal{O}(\log n)$
- Sorted array $\mathcal{O}(\log n)$
- List of associations O(n)

Dictionary data structures we have seen, with lookup times and a special case

- Binary search tree $\mathcal{O}(\log n)$
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- List of associations $\mathcal{O}(n)$
- An array using keys (0, 1, ..., k-1) as indices $\mathcal{O}(1)$

The last of these is sometimes called "direct addressing"

We've used direct addressing before

Union-find objects and graph vertices are numbered so that we can use direct addressing to store information about them

Could we use a similar strategy for keys that aren't the first *k* naturals?

Example: phone book

A phone book is a dictionary where the keys are names and the values are phone numbers

How can we use names (strings) as keys?

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How can we use names (strings) as keys?

Let's map strings to small integer keys by using the value of the first character

The first-character hash

(bucket)	name	phone
(0)	"Alice"	555-1212
(1)	0	0
(2)	"Carol"	555-1214
(3)	0	0
	:	

"Yves"

0

(24)

(25)

555-1215

0

The first-character hash

(bucket)	name	phone		
(0)	"Alice"	555–1212		
(1)	0	0		
(2)	"Carol"	555–1214		
(3)	0	0		
(24)	"Yves"	555–1215		
(25)	0	0		

What happens when we want to add Charles to the phonebook?

Hash collision!

The function that maps names to numbers is called a *hash function*:

$$h("Alice") = 0$$

 $h("Carol") = 2$

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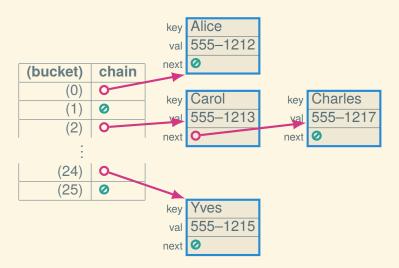
$$h("Charles") = 2$$

How do we resolve it?

Two solutions to hash collision

- 1. Store a linked list in each bucket (separate chaining)
- 2. Use the next free bucket instead (open addressing)

Separate chaining hash table



Open addressing hash table

(bucket)	name	phone
(0)	"Alice"	555–1212
(1)	0	0
(2)	"Carol"	555–1214
(3)	"Charles"	555–1217
(4)	0	0

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(24)	"Yves"	555-1215
(25)	0	0

What happens as the table fills up

- Separate chaining: the length of the chains is $\mathcal{O}(n)$
- Open addressing: the length of the scan is O(n)

Thus, it's important to have enough buckets

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Here's a better hash function:

Input: A string str and number of buckets buckets Output: A hash code between 0 and buckets - 1

 $hash \leftarrow 1;$

for each character c in str do | $hash \leftarrow 31 \times hash + c$ end

return hash % buckets

What makes a good hash function?

Hash functions are big topic—what you need to know:

- deterministic (not random)
- uniform (not clustery)

Load

For good performance, we can't let the table get too full One way to think of this is the *load factor*:

load factor =
$$\frac{n}{k}$$

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For separate chaining, we should keep the load factor < 2 For open addressing, we should keep the load factor < 0.75

Resizing

When the load factor gets too high, we need to grow the table

- Requires rehashing everything!
- \bullet Grow geometrically (like dynamic array), so amortized time remains $\mathcal{O}(1)$

Next time: random BSTs